



## Diffusion LLMs (dLLMs) & Reinforcement Learning (RL)

■ **Goal:** Improve reasoning of dLLMs with an RL method tailored to masked diffusion structure.

**Masked diffusion models** learn the conditional distribution: input partially masked sequence  $\mathbf{x} = (x_1, \dots, x_D)$ , output  $\pi_\theta(\mathbf{x}) \in \mathbb{R}^{D \times V}$ , where (“UM” = unmasked)

$$\pi_\theta(\mathbf{x})_{d,u} \approx \Pr_{\mathbf{X} \sim p_{\text{data}}}(X_d = u | \mathbf{X}_{\text{UM}} = \mathbf{x}_{\text{UM}}), \text{ if } x_d = \text{M}.$$

Sequence probability defined by **random-order autoregressive** generation:

$$p_\theta(\mathbf{x}) = \mathbb{E}_\sigma p_\theta(\mathbf{x}; \sigma), \text{ where } p_\theta(\mathbf{x}; \sigma) = \prod_{d=1}^{|\mathbf{x}|} \pi_\theta(x_{\sigma_d} | \mathbf{x}_{\sigma_{<d}}).$$

**ELBO:** a surrogate of log-probability, defined as below:

$$\begin{aligned} -\log p_\theta(\mathbf{x}) &= -\log \mathbb{E}_\sigma p_\theta(\mathbf{x}; \sigma) \leq -\mathbb{E}_\sigma \log p_\theta(\mathbf{x}; \sigma) \\ &= \mathbb{E}_{m \sim \text{Unif}\{1, \dots, |\mathbf{x}|\}} \left[ \frac{|\mathbf{x}|}{m} \mathbb{E}_{\mu_m(\tilde{\mathbf{x}}|\mathbf{x})} \sum_{d: \tilde{x}_d = \text{M}} -\log \pi_\theta(\tilde{\mathbf{x}})_{d, x_d} \right] =: \mathcal{L}_\theta(\mathbf{x}), \end{aligned}$$

where  $\mu_m(\cdot|\mathbf{x})$  means to sample a uniformly random subset of  $\{1, \dots, |\mathbf{x}|\}$  of size  $m$  and mask the corresponding entries in  $\mathbf{x}$ . With i.i.d. samples from  $p_{\text{data}}$ , the **denoising cross-entropy** loss for training MDM is simply  $\min_\theta \mathbb{E}_{p_{\text{data}}(\mathbf{x})} \mathcal{L}_\theta(\mathbf{x})$ .

For reasoning tasks, we write a sequence as  $\mathbf{x} = (\mathbf{q}, \mathbf{o})$  (prompt, response).

■ **Why existing RL methods for LLMs are suboptimal for dLLMs?**

- Sequence likelihood is expensive/inexact for bidirectional generation.
- GRPO-style methods are mostly backward-trajectory based.
- Reward maximization alone tends to be mode-seeking.

**Policy Distribution Matching Learning.** Given a pretrained dLLM policy  $\pi_{\text{ref}}(\mathbf{o}|\mathbf{q})$  that samples from a distribution  $p_{\text{ref}}(\mathbf{o}|\mathbf{q})$ , a reward function  $r : (\mathbf{q}, \mathbf{o}) \mapsto \mathbb{R}$ , a set of prompts  $\mathcal{D}$ , and temperature  $\alpha > 0$ , learn a dLLM policy  $\pi_\theta(\mathbf{o}|\mathbf{q})$  to produce the desired optimal distribution  $p_*(\mathbf{o}|\mathbf{q})$

$$p_*(\mathbf{o}|\mathbf{q}) \propto p_{\text{ref}}(\mathbf{o}|\mathbf{q}) \exp\left(\frac{r(\mathbf{q}, \mathbf{o})}{\alpha}\right) \text{ via } \min_{\pi_\theta} \mathbb{E}_{\mathbf{q} \sim \mathcal{D}} \mathcal{F}(p_\theta(\cdot|\mathbf{q}), p_*(\cdot|\mathbf{q})).$$

## Distribution Matching Policy Optimization (DMPO)

► **Core loss: Weighted Denoising Cross-Entropy (WDCE)** [5]:

$$\min_{\theta} \mathbb{E}_{\mathbf{q} \sim \mathcal{D}} \mathbb{E}_{\sigma} \mathbb{E}_{p_{\text{old}}(\mathbf{o}|\mathbf{q}; \sigma)} \left\{ w(\mathbf{o}|\mathbf{q}; \sigma) \mathbb{E}_{m \sim \text{Unif}\{1, \dots, |\mathbf{o}|\}} \left[ \frac{|\mathbf{o}|}{m} \mathbb{E}_{\mu_m(\tilde{\mathbf{o}}|\mathbf{o})} \sum_{d: \tilde{o}_d = \text{M}} -\log \pi_\theta(\tilde{\mathbf{o}})_{d, \tilde{o}_d} \right] \right\}.$$

Treating i.i.d. samples from the old policy  $p_{\text{old}}$  as **weighted** samples from the optimal policy  $p_*$ : compute the **weights** by

$$w(\mathbf{o}|\mathbf{q}; \sigma) = \frac{p_*(\mathbf{o}|\mathbf{q}; \sigma)}{p_{\text{old}}(\mathbf{o}|\mathbf{q}; \sigma)} \propto \exp\left(\frac{r(\mathbf{q}, \mathbf{o})}{\alpha} + \log \frac{p_{\text{ref}}(\mathbf{o}|\mathbf{q}; \sigma)}{p_{\text{old}}(\mathbf{o}|\mathbf{q}; \sigma)}\right) =: e^{\ell(\mathbf{o}|\mathbf{q}; \sigma)},$$

► **Small-batch issue & fix.** All-positive weights may promote both good and bad responses when rollouts per prompt are limited. We insert negative gradients by baseline subtraction:

$$w_{\text{real}}(\mathbf{o}|\mathbf{q}; \sigma) = w(\mathbf{o}|\mathbf{q}; \sigma) - w_{\text{base}}(\mathbf{o}|\mathbf{q}; \sigma).$$

The simplest one is  $w_{\text{base}}(\mathbf{o}|\mathbf{q}; \sigma) = 1$ .

► Besides WDCE (forward KL style), we also explore **weighted direct discriminative optimization (WDDO)** [4]:

$$\mathcal{F} = -\mathbb{E}_{\sigma} \mathbb{E}_{p_{\text{old}}(\mathbf{o}|\mathbf{q}; \sigma)} \left[ w(\mathbf{o}|\mathbf{q}; \sigma) \log \sigma \left( \log \frac{p_\theta(\mathbf{o}|\mathbf{q})}{p_{\text{old}}(\mathbf{o}|\mathbf{q})} \right) + \log \sigma \left( -\log \frac{p_\theta(\mathbf{o}|\mathbf{q})}{p_{\text{old}}(\mathbf{o}|\mathbf{q})} \right) \right],$$

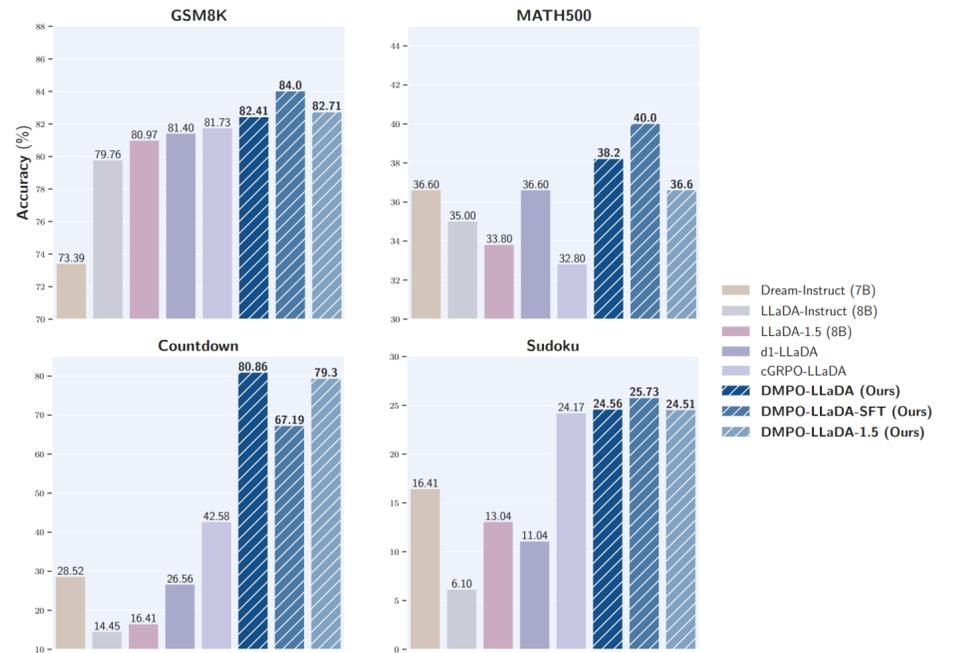
which naturally introduces positive/negative gradient competition and shares the same optimum  $p_*$ .

► **Practical properties of DMPO.**

- **Off-policy:** supports replay buffer and stale roll-out reuse.
- **Forward-only:** training leverages cheap noising, not full trajectories.

## Results: Strong Reasoning Gains & Efficient Training

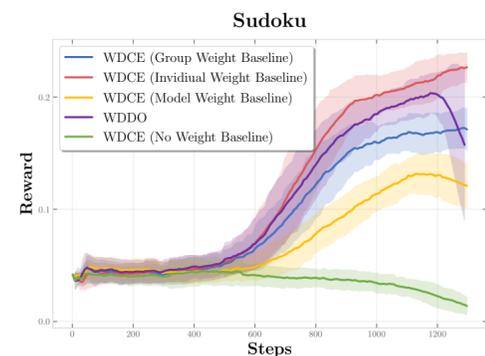
◆ **Main benchmark comparison (four tasks, three generation lengths):**



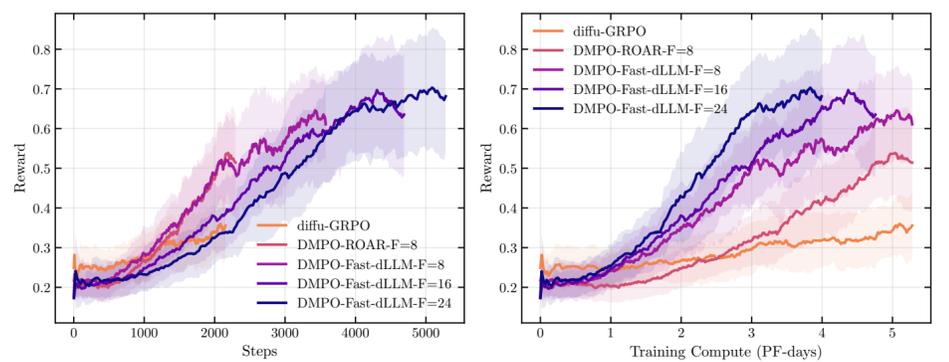
- DMPO consistently outperforms dLLM baselines on GSM8K, MATH500, Countdown, and Sudoku.
- Versus d1 [3] & cGRPO [1], gains are especially large on planning-heavy tasks (Countdown/Sudoku).

◆ **Ablation and compute efficiency:**

◇ Baseline subtraction is crucial for stable learning at small batch size.



◇ DMPO is sample-efficient (buffer reuse) and compute-efficient (benefits from fast-dLLM [2] sampling).



## References

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